

次の極限值を求めよ。(No. 1)

$$(1) \lim_{n \rightarrow \infty} \frac{1}{n} \left(\sin \frac{\pi}{2n} + \sin \frac{2\pi}{2n} + \sin \frac{3\pi}{2n} + \cdots + \sin \frac{n\pi}{2n} \right)$$

$$(2) \lim_{n \rightarrow \infty} \frac{1}{\sqrt{n}} \left(\frac{1}{\sqrt{n+1}} + \frac{1}{\sqrt{n+2}} + \frac{1}{\sqrt{n+3}} + \cdots + \frac{1}{\sqrt{2n}} \right)$$

$$(3) \lim_{n \rightarrow \infty} \frac{\pi}{n} \left(\sin^3 \frac{\pi}{n} + \sin^3 \frac{2\pi}{n} + \sin^3 \frac{3\pi}{n} + \cdots + \sin^3 \frac{n\pi}{n} \right)$$

$$(4) \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{1}{n} \sin^2 \frac{\pi k}{4n}$$

$$(5) \lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=1}^n \frac{k}{\sqrt{n^2 + k^2}}$$

$$(6) \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k}{n^2 + k^2}$$

$$(7) \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{n}{(n+k)(3n+k)}$$

$$(8) \lim_{n \rightarrow \infty} \frac{1}{n} (\sqrt[n]{e} + \sqrt[n]{e^2} + \sqrt[n]{e^3} + \cdots + \sqrt[n]{e^n})$$

$$(9) \lim_{n \rightarrow \infty} \left(\frac{a}{n+a} + \frac{a}{n+2a} + \frac{a}{n+3a} + \cdots + \frac{a}{n+na} \right) \quad (\text{ただし, } a \text{ は正の定数})$$