

次の極限值を求めよ。(No. 2)

$$(1) \lim_{n \rightarrow \infty} \left[\log \left\{ (n+1)(n+2)(n+3) \cdots (n+n) \right\}^{\frac{1}{n}} - \log n \right]$$

$$(2) \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k}{n^2} \cos \left(\frac{k^2 \pi}{2n^2} \right)$$

$$(3) \lim_{n \rightarrow \infty} \int_0^{1/n-1} \sum_{k=0}^{n-1} x^{2n+k} dx$$

$$(4) \lim_{n \rightarrow \infty} \frac{(1+2+3+\cdots+n)^5}{(1+2^4+3^4+\cdots+n^4)^2}$$

$$(5) \lim_{n \rightarrow \infty} \frac{1}{n} \log \left\{ \frac{n}{n} \times \frac{n+2}{n} \times \frac{n+4}{n} \times \cdots \times \frac{n+2(n-1)}{n} \right\}$$

$$(6) \lim_{n \rightarrow \infty} \frac{1}{n^6} \sum_{k=n+1}^{2n} k^5$$